

## Gravitational Potential Energy

Potential Energy is the stored energy that an object has that can be released into another form of energy.

Examples: chemical: gasoline, food, batteries  
elastic: trampoline, bow

Gravitational Potential Energy,  $E_g$ , is energy stored as the result of the vertical position (height) of an object.

Gravitational Energy is always measured... relative to a reference point  
ie. ground level or an arbitrary location eg. top of a cliff

Measured in J,  $E_g$  depends on an object's mass and height according to:

$$E_g = mgh \quad \text{or} \quad \boxed{E_g = mg \Delta y} \quad \left\{ \begin{array}{l} \text{especially if} \\ \text{using} \end{array} \right.$$

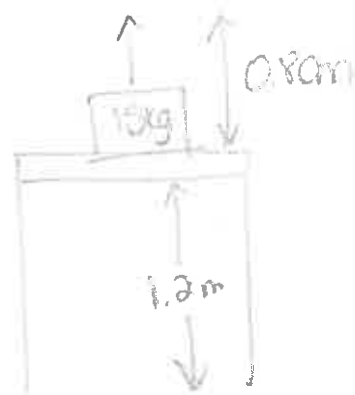
Example: A 15.0 kg textbook is sitting on a 1.20 m tall table. If the book is lifted 0.80 m above the table, how much gravitational potential energy does it have:

a. with respect to the table?

$$\begin{aligned} E_g &= mg \Delta y \\ &= 15 \text{ kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2} \cdot 0.80 \text{ m} \\ &= \boxed{120 \text{ J}} \end{aligned}$$

b. with respect to the floor?

$$\begin{aligned} E_g &= mg \Delta y \\ &= 15 \cdot 9.8 \cdot 2 \text{ m} \\ &= 294 \text{ J} = \boxed{290 \text{ J}} \end{aligned}$$



Example: How high would you have to lift a 1500kg truck to give it a potential energy of 3100 J?

$$\begin{aligned} E_g &= mg \Delta y \\ \Delta y &= \frac{E_g}{mg} = \frac{3100 \text{ J}}{1500 \text{ kg} \cdot 9.8 \frac{\text{m}}{\text{s}^2}} = \boxed{0.21 \text{ m}} \end{aligned}$$

Kinetic energy and potential energy have a close relationship, as one form often transforms into the other as work is done. Example: basketball is picked up then dropped - potential energy converted into kinetic

This illustrates the Law of Conservation of Energy:

energy is neither created nor destroyed, it simply changes forms.

Thus, the sum of the kinetic energy and potential energy (known as Total Mechanical Energy,  $E_T$ ), remains constant in any (isolated or closed) system.

$$E_T = E_g + E_k$$

Example: a. Determine the total mechanical energy of a 48 g golf ball if it has a velocity of 25 m/s when it leaves a golf club.

Given:  $m = 48\text{g} = 0.048\text{kg}$   
 $1000\text{g}/\text{kg}$   
 $v_f = 25\text{m/s}$   
 assume  $\Delta y = 0$

Need:  $E_T$

$$\begin{aligned} E_T &= E_g + E_k \\ &= 0 + \frac{1}{2}mv^2 \\ &= \frac{1}{2}(0.048\text{kg})\left(\frac{25\text{m}}{\text{s}}\right)^2 \\ &= \boxed{15\text{J}} \end{aligned}$$

b. If the golf ball goes in an arc and slows to 15 m/s at the peak of its trajectory, calculate the maximum height of the golf ball. Hint: Use your answer from (a)!



$$\begin{aligned} E_T &= E_g + E_k \\ E_T &= mg\Delta y + \frac{1}{2}mv^2 \end{aligned}$$

$$mg\Delta y = E_T - \frac{1}{2}mv^2$$

$$\Delta y = \frac{E_T - \frac{1}{2}mv^2}{mg} = \frac{15\text{J} - \frac{1}{2}(0.048)(15\text{m/s})^2}{0.048\text{kg} \cdot 9.8\frac{\text{m}}{\text{s}^2}}$$

$$= 20.4\text{m} = \boxed{2.0 \times 10^1\text{m}}$$