

Work and Power

When you think of 'work' you think of... studying, doing homework, a job, etc.

but in physics, work is the energy that a force gives to an object when the force moves the object

In everyday life you do work when... lift your backpack to your shoulders, when you throw a ball

Work can be calculated using:

$$W = F \Delta d \cos \theta$$

Where W = work, measured in N·m or J (joule)

F = magnitude of the applied force, measured in N

Δd = magnitude of displacement, measured in m

θ = the angle between F and Δd

notice work is scalar

Example: A box that weighs 200.0 N is lifted a distance of 0.50 m straight up. How much work is done?

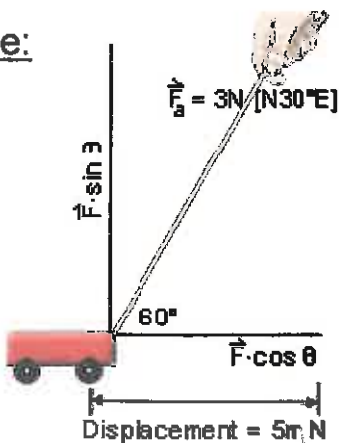
$$\begin{aligned} W &= F \Delta d \cos \theta \\ &= 200 \text{ N} \cdot 0.5 \text{ m} \cdot \cos 0^\circ \\ &= 100 \text{ N} \cdot \text{m} \cdot 1 = \boxed{1.0 \times 10^2 \text{ J}} \end{aligned}$$

When the applied force is in the same direction as the object's displacement...

positive work occurs.

Work is also positive when the direction of the object's displacement is between 0° and 90° to the applied force.

Example:



$$\begin{aligned} W &= F \Delta d \cos \theta \\ &= 3 \text{ N} \cdot 5 \text{ m} \cdot \cos 60^\circ \\ &= 7.5 \text{ N} \cdot \text{m} = \boxed{8 \text{ J}} \end{aligned}$$

What happens when a moving object slides to rest? This means that a force has done...

negative work

Negative work happens when an object moves in a direction opposite to the applied force, due to friction.

Negative work causes a loss of kinetic energy. Forces that cause negative work are exerted at angles between 90° and 180° , opposite to the object's direction.

Example: A 1385 kg car traveling at 61 km/h is brought to a stop while skidding 42 m. What is the work done on the car by frictional forces?

Given: $m = 1385 \text{ kg}$
 $v_i = 61 \text{ km/h} = 16.94 \text{ m/s}$
 $v_f = 0 \text{ m/s}$
 $\Delta d = 42 \text{ m}$

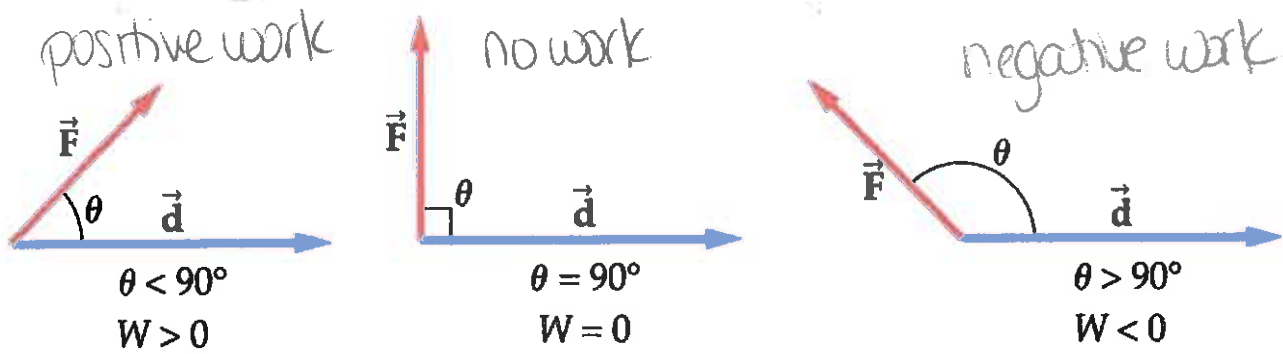
Need: W

Equations:
 $F_f = ma$
 $W = F_f \cdot d$
 $v_f^2 = v_i^2 + 2ad$

Calculations:
 $a = \frac{v_f^2 - v_i^2}{2d} = \frac{0^2 - (16.94 \text{ m/s})^2}{2(42 \text{ m})} = -3.42 \text{ m/s}^2$
 $F_f = 1385 \text{ kg} \cdot (-3.42 \text{ m/s}^2) = -4737 \text{ N}$
 $W = (-4737 \text{ N}) \cdot (42 \text{ m}) = -2.0 \times 10^5 \text{ J}$

When the direction of the object's displacement is exactly 90° to the applied force, the force does:

zero work



There is zero work done on an object when any of the force, displacement, or the cosine of the angle between the force and the displacement is zero. aka 90°

Example: A 3.0 kg pineapple is held 1.2 m above the floor for 15 s. How much work is done on the pineapple?

$$W = F \cdot \Delta d \cdot \cos \theta$$

↑
 zero displacement = zero work or 0 J